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Name: _____

APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY
SIXTH SEMESTER B.TECH DEGREE EXAMINATION, APRIL 2018

Course Code: EE304

Course Name: ADVANCED CONTROL THEORY (EE)

Max. Marks: 100

Duration: 3 Hours

PART A

Answer all questions, each carries 5 marks.

Marks

- 1 What is a lag compensator? Draw its pole-zero plot and the frequency response characteristics. (5)
- 2 Explain the effects of adding PID controller to a system. (5)
- 3 Selecting $i_1(t) = x_1(t)$ and $i_2(t) = x_2(t)$ as state variables obtain state equation and output equation of the network shown in Fig.1 (5)

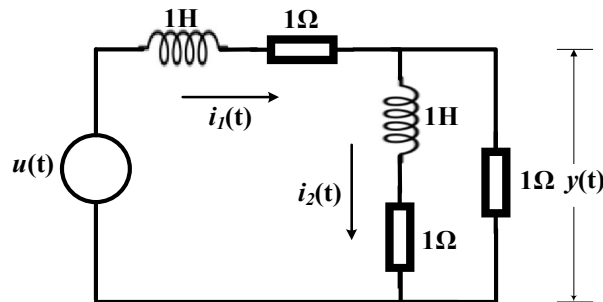


Fig.1

- 4 The characteristic polynomial of certain sampled data system is given by $P(z) = z^4 - 1.2z^3 + 0.07z^2 + 0.3z - 0.08 = 0$, test the stability of the system using Jury's stability test. (5)
- 5 Explain different non linearities with diagram. (5)
- 6 What is limit cycle? How will you determine stable and unstable limit cycle using phase portrait? (5)
- 7 What are singular point? Explain the types of singular point. (5)
- 8 Determine given quadratic form is positive definite or not (5)

$$V(x) = 10x_1^2 + 4x_2^2 + x_3^2 + 2x_1x_2 - 2x_2x_3 - 4x_1x_3$$

PART B

Answer any two full questions, each carries 10 marks.

- 9 a) For a feedback system shown in Fig. 2, design suitable compensator so that phase margin is 40° and steady state error for ramp input ≤ 0.2 (10)

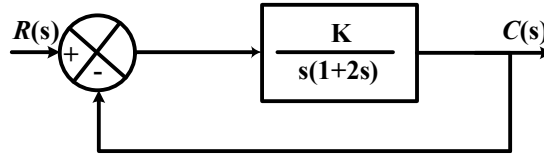


Fig. 2

- 10 Design a suitable compensator for the system with open-loop transfer function (10)

$$G(s)H(s) = \frac{1}{s(s+1)(s+2)}$$
 so that the over shoot to a unit step input to be limited to 20% and the transient to be settled with in 3s.
- 11 a) Briefly explain Ziegler – Nichol’s PID tuning rules. (6)
 b) Write the design steps of lead compensator based on frequency domain approach. (4)

PART C

Answer any two full questions, each carries 10 marks.

- 12 Find the complete response of the system (10)

$$\dot{x} = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix} x + \begin{bmatrix} 2 & 1 \\ 0 & 1 \end{bmatrix} U(t), x(0) = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

and $y(t) = \begin{bmatrix} 1 & 0 \\ 1 & 1 \end{bmatrix} x$ to the following input, $U(t) = \begin{bmatrix} u(t) \\ e^{3t}u(t) \end{bmatrix}$ where $u(t)$ is the unit step input.

- 13 a) Transform the system in to controllable canonical form (7)

$$\dot{x} = \begin{bmatrix} -1 & 1 \\ 0 & 2 \end{bmatrix} x + \begin{bmatrix} 2 \\ 1 \end{bmatrix} u \text{ and } y = [1 \quad 2]x$$

- b) State and explain sampling theorem (3)

- 14 a) Consider a system defined by (7)

$$\dot{x} = \begin{bmatrix} 0 & 1 \\ -3 & 1 \end{bmatrix} x + \begin{bmatrix} 0 \\ 2 \end{bmatrix} u \text{ and } y = [1 \quad 0]x$$

Using state feedback control $u = -Kx$, it is desired to have the closed loop poles at $s = -3$ and $s = -4$, determine the state feedback gain matrix K .

- b) What is pulse transfer function? (3)

PART D

Answer any two full questions, each carries 10 marks.

- 15 Obtain the describing function of saturation non-linearity (10)
- 16 A common form of an electronic oscillator is represented as shown in Fig. 3. For (10)
 what value of K , the possibility of limit cycle predicted? If $K=3$, determine amplitude and frequency of limit cycle. Also find the maximum value of K for the

system is stable.

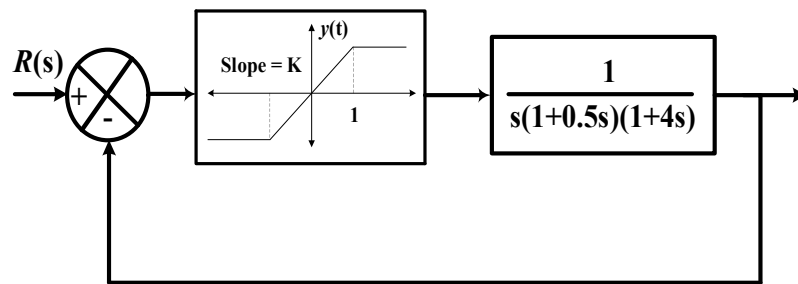


Fig. 3

17

A second order system is represented by $\dot{x} = Ax$ where

(10)

$$A = \begin{bmatrix} 0 & 1 \\ -1 & -1 \end{bmatrix}$$

Assuming matrix Q to be identity matrix, solve for matrix P in the equation $A^T P + P A = -Q$. Use Lyapunov theorem and determine the stability of the system. Write the Lyapunov function $V(x)$

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APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY
SIXTH SEMESTER B.TECH DEGREE EXAMINATION(R&S), MAY 2019

Course Code: EE304

Course Name: ADVANCED CONTROL THEORY

Max. Marks: 100

Duration: 3 Hours

PART A

Answer all questions, each carries 5 marks.

Marks

- | | | |
|---|--|-----|
| 1 | Compare the effects of P, PI and PID controllers on the closed loop system performance in terms of rise time, peak overshoot, settling time, steady state error and stability. | (5) |
| 2 | What are the effects of Lag and Lead compensators on the system performance? | (5) |
| 3 | Explain the terms (i) state (ii) state variables (iii) state vector (iv) state space (v) state trajectory of a system. | (5) |
| 4 | What is pulse transfer function? Derive the transfer function of a ZOH circuit. | (5) |
| 5 | State any five characteristics of Nonlinear systems. | (5) |
| 6 | Define Describing function. Explain how describing function can be used for stability analysis of nonlinear systems. | (5) |
| 7 | Define Singular point. Explain the nature of Eigen values of system matrix for any five types of singular points. | (5) |
| 8 | Explain Liapunov second method of stability for nonlinear systems. | (5) |

PART B

Answer any two full questions, each carries 10 marks.

- | | | |
|----|---|------|
| 9 | A unity feedback system has an open loop transfer function $G(S) = K/[S(1+2S)]$. Design a suitable lag compensator so that phase margin is 40° and the velocity error constant is 5. | (10) |
| 10 | Design a lead compensator for a unity feedback system with open loop transfer function $G(S) = K/[S(S+8)]$ to satisfy the following specifications. (1) Percentage overshoot = 9.5% (2) Natural frequency of oscillation=12 rad/sec (3) Velocity error constant ≥ 10 . | (10) |
| 11 | a) Explain the Ziegler-Nichols method of tuning a PID controller. | (6) |
| | b) What is meant by series compensation and feedback compensation in control systems? | (4) |

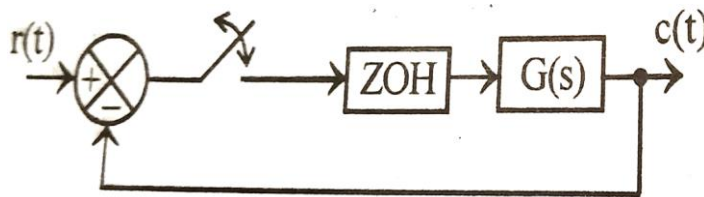
PART C

Answer any two full questions, each carries 10 marks.

12 a) Define controllability and observability of a system and check whether the system $\frac{Y(s)}{U(s)} = \frac{1}{(s+1)(s+2)}$ is controllable or not. (6)

b) Check the stability of the sampled data control system shown below (4)
 $z^3 - 0.2z^2 - 0.25z + 0.05 = 0$

13 Determine the pulse transfer function of the discrete time control system shown in figure for a sampling time of $T=1$ sec. Also find the response to unit step input. The transfer function of the system is $G(s) = 1/(s+1)$. (10)



14 a) Derive the state model of an R-L-C series circuit (3)

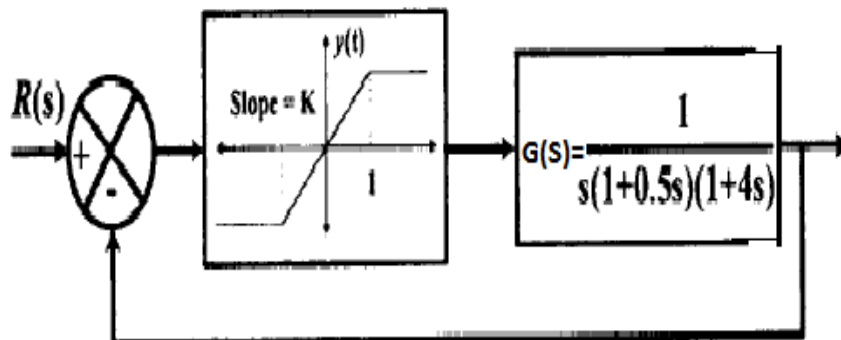
b) Consider a linear system described by the transfer function $Y(s)/U(s) = 10/[S(S+1)(S+2)]$. Design a feedback controller with a state feedback so that the closed loop poles are placed at $-2, -1 \pm j1$. (7)

PART D

Answer any two full questions, each carries 10 marks.

15 Derive the Describing function of saturation with Dead-zone nonlinearity. (10)

16 Consider a unity feedback system shown in figure having a saturating amplifier with a gain K. Determine the maximum value of K for the system to be stable. What would be the frequency and nature of limit cycle for a gain of $K=2.5$? (10)



17 A linear second order system is described by the equation $\ddot{e} + 2\delta\omega_n\dot{e} + \omega_n^2e = 0$ (10)

Where $\delta = 0.15$, $\omega_n = 1\text{rad/sec}$, $e(0)=1.5$, and $\dot{e}(0) = 0$

Determine the singular point and state the stability by constructing the phase trajectory using the method of isoclines.

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APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY
SIXTH SEMESTER B.TECH DEGREE EXAMINATION(S), DECEMBER 2019

Course Code: EE304

Course Name: ADVANCED CONTROL THEORY

Max. Marks: 100

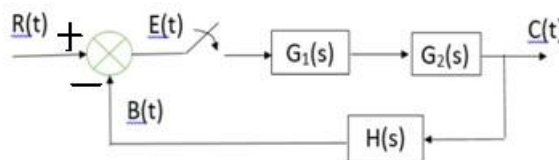
Duration: 3 Hours

PART A

Answer all questions, each carries 5 marks.

Marks

- | | | |
|---|--|-----|
| 1 | Obtain the transfer function of a lead compensator with the help of an electrical network. | (5) |
| 2 | Derive the transfer function of a PID Controller | (5) |
| 3 | Derive a relation between state equation and transfer function for LTI system. | (5) |
| 4 | Obtain the pulse transfer function for the system shown below. | (5) |



- | | | |
|---|---|-----|
| 5 | With a neat diagram explain how the describing function analysis is used to determine the stability of a system? | (5) |
| 6 | What are jump response and limit cycles in connection with nonlinear systems? | (5) |
| 7 | Explain with neat diagram, what is phase trajectory and phase portrait? | (5) |
| 8 | Define positive definite and positive semi definite functions according to Liapunov stability criteria, with suitable examples. | (5) |

PART B

Answer any two full questions, each carries 10 marks.

- | | | |
|----|--|------|
| 9 | a) Draw the bode-plot of lag compensator and obtain an expression for maximum phase lag and corresponding frequency. | (6) |
| | b) Explain turning of PID controller using Ziegler-Nichols tuning method. | (4) |
| 10 | Explain the procedure for design of a lag Compensator using Bode Plot with suitable example | (10) |
| 11 | Consider a unity feedback system with open loop transfer function | (10) |

$$G(s) = \frac{k}{s(s+8)}$$

Design a lead compensator to meet the following specification:

1. Percentage peak overshoot is 9.5%
2. Natural frequency of oscillations 12 rad/sec
3. Velocity error constant ≥ 10

PART C

Answer any two full questions, each carries 10 marks.

- 12 a) A system is described by $\dot{x}(t) = \begin{bmatrix} 0 & 1 \\ -4 & -4 \end{bmatrix} x(t)$ (5)

Determine state transition matrix for the system.

- b) Define controllability. Explain with a suitable example, how can we check the controllability of a system? (5)

- 13 Derive the state model of the following transfer function in, (10)

(i) Controllable canonical form

(ii) Diagonal canonical form

$$\frac{y(s)}{u(s)} = \frac{5(s+2)}{s(s+1)(s+3)}$$

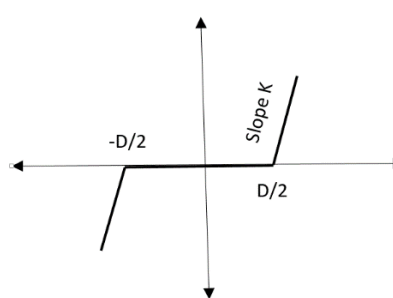
- 14 Examine the stability of the system with the following characteristic equation (10) using Jury's stability test.

$$z^4 - 1.2z^3 + 0.07z^2 + 0.3z - 0.08 = 0$$

PART D

Answer any two full questions, each carries 10 marks.

- 15 Identify the following non linearity and derive a describing function for the same (10)



- 16 Consider the following non linear differential equation. (10)

$$\ddot{y} - \left(0.1 - \frac{10}{3} \dot{y}^2\right) \dot{y} + y + y^2 = 0$$

Find all singular points of the system, classify them and sketch the phase portrait in the neighbourhood of singular points.

- 17 a) Discuss any three non linearities present in nature. (6)

- b) Investigate the stability of the following non-linear system using Liapunov direct method (4)

$$\dot{x}_1 = x_2$$

$$\dot{x}_2 = -x_1 - x_1^2 x_2.$$

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APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY

Sixth semester B.Tech examinations (S), September 2020

Course Code: EE304**Course Name: ADVANCED CONTROL THEORY**

Max. Marks: 100

Duration: 3 Hours

PART A*Answer all questions, each carries 5 marks.*

- | | | Marks |
|---|--|-------|
| 1 | What is a PI controller? What are its effects on the system performance? | (5) |
| 2 | What is a lead compensator? Obtain its frequency response characteristics | (5) |
| 3 | What is state space? What are the advantages of state space analysis? | (5) |
| 4 | What is pulse transfer function? What is the stability criterion of a sampled data control system? | (5) |
| 5 | Mention any two characteristics of Nonlinear systems. What are limit cycles? | (5) |
| 6 | Define Describing function. What is the difference between stability analysis of linear and nonlinear systems? | (5) |
| 7 | What is the difference between describing function and phase plane method of stability analysis? | (5) |
| 8 | Explain Liapunov direct method of stability for nonlinear systems. | (5) |

PART B*Answer any two full questions, each carries 10 marks.*

- | | | |
|----|--|------|
| 9 | The open loop transfer function of a unity feedback control system is given by $G(S) = K/[S(1+0.5S)(1+0.2S)]$. It is desired that (i) the steady state error to unit ramp input is less than 0.125 (ii) Phase margin $\geq 30^\circ$ (iii) Gain margin ≥ 10 db. Design a suitable compensator. | (10) |
| 10 | Design a suitable compensator for a unity feedback system with open loop transfer function $G(S) = K/[S(S+4)(S+7)]$ to satisfy the following specifications. (1) Percentage overshoot = 12.63% (2) Natural frequency of oscillation = 8 rad/sec (3) Velocity error constant ≥ 2.5 . | (10) |
| 11 | Explain the Ziegler-Nichols method of tuning a PID controller when (a) dynamic model is known (b) dynamic model is not known. | (10) |

PART C*Answer any two full questions, each carries 10 marks.*

- 12 a) Obtain the state model of the system whose transfer function is given by (5)
 $Y(s)/U(s) = 10/[s^3 + 4s^2 + 2s + 1]$
- b) Obtain the state model of a field controlled DC motor. (5)
- 13 A discrete time system is described by the difference equation (10)
 $y(k+2) + 5y(k+1) + 6y(k) = u(k)$
 $y(0) = y(1) = 0; T = 1 \text{ sec.}$
 (a) Determine state model in a canonical form (b) Find the state transition matrix
- 14 Check the stability of the sampled data control system with the following characteristic equation using Jury's stability test $z^4 - 1.7z^3 + 1.04z^2 - 0.268z + 0.024 = 0$ (10)

PART D*Answer any two full questions, each carries 10 marks.*

- 15 Derive the Describing function of saturation with deadzone. (10)
- 16 Construct the phase trajectory for the system (10)
 $\dot{x}_1 = x_2, \dot{x}_2 = -\text{sign}(x_1)$ where $\text{sign}(x_1) = \begin{cases} 1 & \text{for } x_1 > 0 \\ -1 & \text{for } x_1 \leq 0 \end{cases}$ starting from (2,0)
- 17 Test the stability of the system using Lyapunov stability theorem (10)
 (a) $\dot{x}_1 = -x_1 + 2x_1^2x_2, \dot{x}_2 = -x_2$
 (b) $\dot{x}_1 = x_2, \dot{x}_2 = -\sin(x_1) - x_2$
